

1. In simple linear regression, both the t and F tests can be used as model utility tests.
- ☐ True
- ☐ False
2. The sample correlation coefficient is a measure of the strength of a linear relationship between two continuous variables.
- ☐ True
- ☐ False
3. Many factors affect the length of a professional football game. A study was conducted to determine the relationship between the total number of penalty yards (x) and the time required to complete a game (y , in hours). The following is the summary data:
 $n = 9$, $S_{XX}=26,256$, $S_{YY}=3.956$, $S_{XY}=244.8$, $MSE = 0.2390$
The expected value of the slope is _____. (6 decimal places)

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The 95% confidence interval for the slope is (_____ , _____) (6 decimal places)

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 $n = 9$, $S_{XX}=26,256$, $S_{YY}=3.956$, $S_{XY}=244.8$, $MSE = 0.2390$.
For a t-test for the association of time vs penalty yards with a significance level of 0.05, Which of the following are the correct hypotheses:

- ☐ $H_0: \beta_0 = 0$, $H_a: \beta_0 \neq 0$
- ☐ $H_0: \beta_1 = 0$, $\beta_1 > 0$
- ☐ $H_0: \beta_0 = 0$, $\beta_0 > 0$
- ☐ $H_0: \beta_1 = 0$, $H_a: \beta_1 \neq 0$.

The test statistic is _____ (3 decimal places).

The conclusion is:

- ☐ There is an association between length of the game and the number of penalty yards.
- ☐ There is no association between length of the game and the number of penalty yards.

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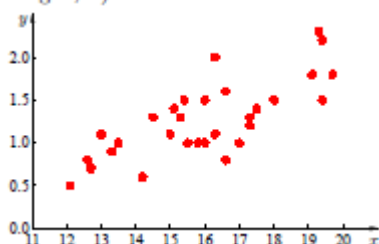
Source of Variation	Sum of Squares	Degrees of freedom	Mean Square
Regression	2.2824	1	2.2824
Error	1.6731	7	0.2390
Total	3.9556	8	

For a F-test for the association of time vs penalty yards with a significance level of 0.05, Which of the following are the correct hypotheses:

- ☐ $H_0: \beta_1 = 0$, $H_a: \beta_1 \neq 0$.
- ☐ H_0 : there is an association between time and penalty yards.
 H_a : There is no association between time and penalty yards.
- ☐ H_0 : There is no association between time and penalty yards.
 H_a : there is an association between time and penalty yards.
- ☐ $H_0: \beta_0 = 0$, $H_a: \beta_0 \neq 0$.

The value of the test statistic is ____ (2 decimal places)

4. Crimini mushrooms are more common than white mushrooms, and they contain a high amount of copper, which is an essential element according to the U.S. Food and Drug Administration. A study was conducted to determine whether the weight of a mushroom is linearly related to the amount of copper it contains. A random sample of crimini mushrooms was obtained, and the weight (in grams) and the total copper content (in mg) was measured for each. The scatterplot is show below:



The summary statistics are: $S_{xx}=137.48$, $S_{yy}=5.7787$, $S_{xy}=21.275$

The sample correlation coefficient is _____. (4 decimal places).

5. The temperature of the upper layer of ocean water is affected by sunlight and wind. There is often a very sharp difference in temperature between the surface zone and the more stationary deep zone. The thermocline layer marks the abrupt drop-off in temperature. The following data were obtained in a study of temperature (x , measured in $^{\circ}\text{C}$) versus depth (y , measured in meters) above the thermocline layer in the Mediterranean Sea.

The ANOVA table from the data is:

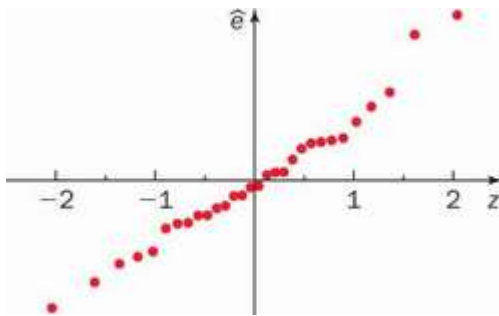
source	SS	df	MS
Regression	108.54	1	108.54
Error	78.06	6	13.01
Total	186.6	7	

The equation of the line is: $\hat{y} = 23.091 - 0.084 x$

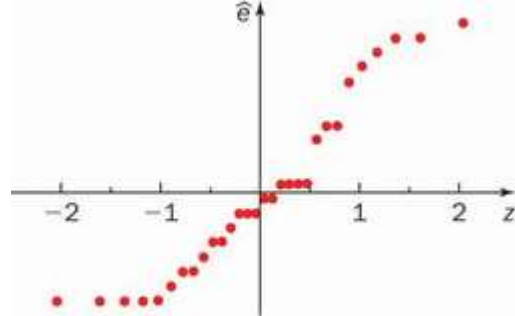
The correlation coefficient is _____ (4 decimal places).

6. The following are four QQ-plots of the residuals from different data sets. For which of these plots is the normality assumption valid?

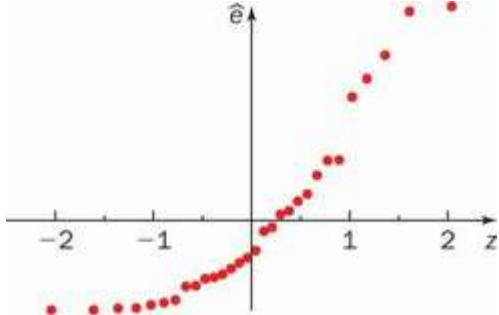
A.



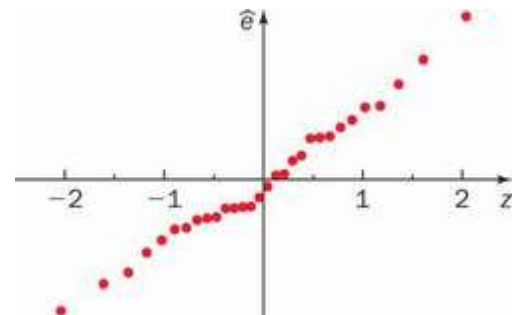
B.



C.



D.



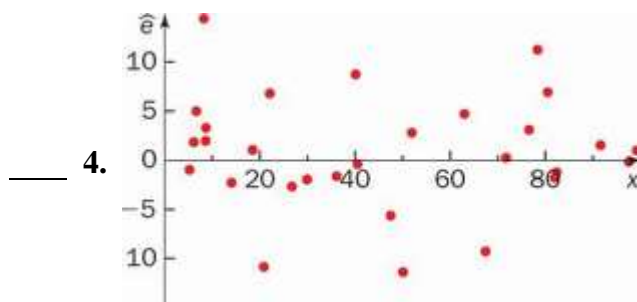
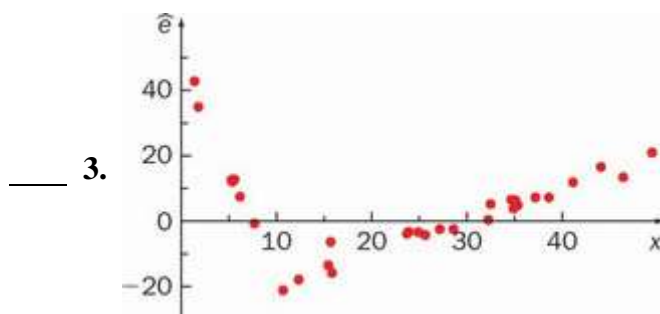
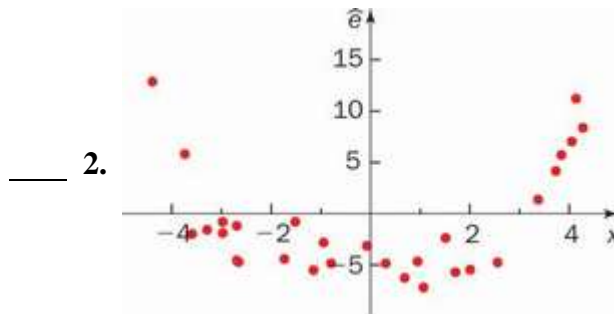
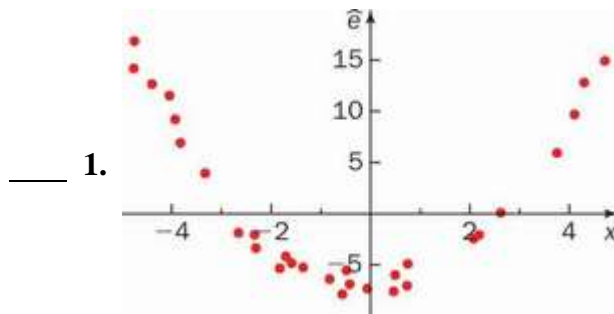
☐ a. A

☐ b. B

☐ c. C

☐ d. D

7. The following are residual plots (residuals versus predictor variable) for different data sets. Please match them with the options available.



- a. The data violates the linear assumption.
- b. The data violates both the linear assumption and constant variance.
- c. The data violates neither the linear assumption nor the constant variance assumption.
- d. The data violates the constant variance assumption.
- e. The data violates only the linear assumption.

8. For $x = x^*$ and a fixed confidence level, a prediction interval for an observed value Y is wider than a confidence interval for the mean value of Y .

- ☐ True
- ☐ False

9. For a fixed confidence level, the width of a confidence interval for the mean value of Y is the same for any value of x^* .
- ☐ True
- ☐ False
10. For $x = x^*$, a confidence interval for the mean value of Y and a prediction interval for an observed value of Y are centered at the same value.
- ☐ True
- ☐ False
11. A new solar collector is being tested for use in charging batteries that can provide electricity for an entire home. A random sample of days was selected and the amount of solar radiation was measured (x , in langleys) for each. The total battery charge was measured as a proportion (y , between 0 and 1). The summary statistics are given.

$$\begin{array}{lll} \hat{\beta}_0 = 0.2007 & n = 21 & \text{MSE} = 0.06135 \\ \hat{\beta}_1 = 0.00446 & \bar{x} = 103.095 & S_{xx} = 12335.8 \end{array}$$

Fill in the blanks. (Give your answer to five decimal places.)

The 95% confidence interval for the slope is (____ , ____).

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The 95% confidence interval for the mean value at the amount of solar radiation of 130 langleys is (____ , ____)

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Fill in the blanks. (Give your answer to four decimal places.)

The 95% confidence interval for the observed value at the amount of solar radiation of 130 langleys is (_____ , _____)